

EJERCICIO FQ1BE2647:

$$m_s = 1000 \text{ kg}$$

$$T = 90 \text{ minutos} = 90.60 \text{ s}$$

$$G = 6,67 \cdot 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}$$

$$R_T = 6370 \text{ km}$$

$$M_T = 5,98 \cdot 10^{24} \text{ kg}$$

a) Altura sobre la Tierra:

$$F_g = m \cdot a_n$$

$$G \frac{M_T}{R^2} = m \cdot \frac{v^2}{R} \Rightarrow v^2 = \frac{GM}{R}$$

$$\left(\frac{2\pi R}{T} \right)^2 = \frac{GM}{R}$$

$$\frac{4\pi^2 R^2}{T^2} = \frac{GM}{R} \Rightarrow \boxed{R^3 = \frac{GM}{4\pi^2} \cdot T^2}$$

$$R^3 = \frac{6,67 \cdot 10^{-11} \cdot 5,98 \cdot 10^{24}}{4\pi^2} \cdot (90.60)^2$$

$$R^3 = 2,95 \cdot 10^{20} \Rightarrow R = \sqrt[3]{} = 6,65 \cdot 10^6 \text{ m}$$

$$R = R_T + h \Rightarrow h = R - R_T$$

$$h = 6,65 \cdot 10^6 - 6370 \cdot 10^3$$

$$h = 2,8 \cdot 10^5 \Rightarrow \boxed{280 \text{ km} = h}$$

b) Velocidad y aceleración en órbita:

$$v = \sqrt{\frac{GM}{R}} = \sqrt{\frac{6,67 \cdot 10^{-11} \cdot 5,98 \cdot 10^{24}}{6,65 \cdot 10^6}} = \boxed{7744,67 \frac{\text{m}}{\text{s}}}$$

$$a = \frac{v^2}{R} = \frac{7744,67^2}{6,65 \cdot 10^6} = \boxed{9,02 \frac{\text{m}}{\text{s}^2}}$$