

EJERCICIO M2BE3063:

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$$\int \frac{\sqrt[3]{x} - 2\sqrt{x} + 5}{\sqrt{x^3}} dx =$$

$$= \int \frac{\sqrt[3]{x}}{\sqrt{x^3}} dx - \int \frac{2\sqrt{x}}{\sqrt{x^3}} dx + \int \frac{5}{\sqrt{x^3}} dx =$$

$$= \int x^{\frac{1}{3} - \frac{3}{2}} dx - \int \frac{2\sqrt{x}}{x\sqrt{x}} dx + 5 \int x^{-\frac{3}{2}} dx =$$

$$= \int x^{-\frac{7}{6}} dx - 2 \int \frac{1}{x} dx + 5 \int x^{-\frac{3}{2}} dx =$$

$$= \frac{x^{-\frac{7}{6}+1}}{-\frac{7}{6}+1} - 2 \ln x + 5 \cdot \frac{x^{-\frac{3}{2}+1}}{-\frac{3}{2}+1} =$$

$$= \frac{x^{-\frac{1}{6}}}{-\frac{1}{6}} - 2 \ln x + 5 \frac{x^{-\frac{1}{2}}}{-\frac{1}{2}} =$$

$$= -\frac{6}{\sqrt[6]{x}} - 2 \ln x - \frac{10}{\sqrt{x}} =$$

$$= -\frac{6}{\sqrt{x}} \frac{\sqrt[6]{x^5}}{\sqrt[6]{x^5}} - 2 \ln x - \frac{10\sqrt{x}}{\sqrt{x}\sqrt{x}} =$$

$$= \boxed{-\frac{6\sqrt[6]{x^5}}{x} - 2 \ln x - \frac{10\sqrt{x}}{x} + C}$$